# **Vanadate Family as Spin-Gap Systems**

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The structural and magnetic properties of the vanadate family with the chemical formula  $AV_2O_5$  (A = Li, Na, Cs, Mg, and Ca) are reviewed in terms of low-dimensional quantumspin systems. These compounds have layered structures with A cations lying between layers. A structural element common to them is a  $VO<sub>5</sub>$  square pyramid formed by five oxygens surrounding the V ion. Each compound has a structure with a characteristic arrangement of  $VO<sub>5</sub>$  square pyramids formed by the sharing of edges and/or corners. All of these compounds are low-dimensional, spin-1/2 magnets and are spin-gap systems except *γ*-LiV<sub>2</sub>O<sub>5</sub>.  $\alpha'$ -NaV<sub>2</sub>O<sub>5</sub> is a spin-Peierls system with the transition temperature  $T_{SP} = 35$  K and the energy gap  $\Delta = 114$  K. The parameter  $2\Delta/k_BT_{SP} = 3.53$  holds well for the all organic and inorganic spin-Peierls compounds except  $\alpha'$ -NaV<sub>2</sub>O<sub>5</sub> for which the measure is 6.44. This difference suggests that the transition observed in  $\alpha'$ -NaV<sub>2</sub>O<sub>5</sub> is not a conventional spin-Peierls transition but an exotic one. Both  $MgV_2O_5$  and  $CaV_2O_5$  are spin-ladder systems with a similar two-leg ladder structure but the gap energy ( $\sim$ 17 K) observed in MgV<sub>2</sub>O<sub>5</sub> is very small compared with that (~600 K) in CaV<sub>2</sub>O<sub>5</sub>. CsV<sub>2</sub>O<sub>5</sub> is a dimer system with a spin gap of ~160 K.  $\gamma$ -LiV<sub>2</sub>O<sub>5</sub>, which has one-dimensional zigzag chains in the structure, shows neither spin gap nor magnetic order down to 0.5 K.

#### **Contents**



There exist many kinds of vanadium oxides that have manifested a variety of structural and electromagnetic properties. One of the most remarkable features is the metal-insulator transition in the binary vanadium oxides.1 These vanadium oxides had been the core materials in the study of the highly correlated electronic system until the discovery of the high-temperaturesuperconducting cuprates. In these vanadium oxides, vanadium ions have various kinds of oxygen coordination, for example, octahedral, tetrahedral, trigonal, and square pyramidal, etc. A typical vanadium oxide with a square pyramidal coordination is  $V_2O_5$ . It has a layer structure, and the layers are formed by sharing the edges and/or corners of square pyramids VO<sub>5</sub>. The vanadium ions are inside the square pyramids.  $V_2O_5$ can intercalate various kinds of ions between the layers.  $A_xV_2O_5$  with alkaline- or alkaline-earth-metal ions as intercalants (A) has been well known as vanadium oxide bronzes.

The compounds  $AV_2O_5$  (A = Li, Na, Cs, Mg and Ca) are situated as end members of such vanadium oxide bronzes. The sites between the layers in  $AV_2O_5$  are fully occupied by A ions. A structural element common to these vanadium oxides is a  $VO<sub>5</sub>$  square pyramid, and each compound has a characteristic intralayer structure formed by sharing the edges and corners of  $VO<sub>5</sub>$  square pyramids. With the arrangements of the magnetic  $V^{4+}$ ion  $(d^{\text{I}}\mathbf{I}, S = 1/2)$ , these compounds have unique structures as low-dimensional magnets; for examples, onedimensional (1-D) chain, zigzag chain, ladder, and dimer.

Low-dimensional spin systems with  $S = 1/2$  and a singlet ground state are of great interest because of their fundamental quantum nature. These systems have been discovered mainly in copper and nickel compounds. Recent studies have been focused on the cuprates, like, for example,  $CuGeO<sub>3</sub><sup>2</sup>$  for the spin-Peierls system and  $SrCu<sub>2</sub>O<sub>3</sub><sup>3</sup>$  for the two-leg ladder system. Since the discovery of spin-gap in  $CaV<sub>4</sub>O<sub>9</sub>$ ,<sup>4</sup> which is the first realization of a two-dimensional spin-plaquette system, compounds of the vanadate family containing  $VO<sub>5</sub>$ pyramids have been drawing experimentalists' attention to low-dimensional magnetic systems with  $S = 1/2$  V<sup>4+</sup> ions. The vanadium oxides  $AV_2O_5$  have also been extensively studied and have shown various kinds of quantum spin phenomena, such as spin-Peierls transition and spin-gap in the ladder structure. In this article, the structural and magnetic properties of  $AV_2O_5$  $(A = Li, Na, Cs, Mg, and Ca)$  are reviewed in terms of a low-dimensional quantum-spin system.

#### <sup>r</sup>′**-NaV2O5 (Spin-Peiels System)**

 $\alpha'$ -NaV<sub>2</sub>O<sub>5</sub> crystallizes in an orthorhombic cell with the space group  $P2_1$ mn.<sup>5</sup> The schematic crystal struc-



**Figure 1.** Schematic crystal structure of orthorhombic  $\alpha'$ -NaV<sub>2</sub>O<sub>5</sub>. A and B represent the V<sup>4+</sup>O<sub>5</sub> and V<sup>5+</sup>O<sub>5</sub> chains, respectively.

ture of  $\alpha'$ -NaV<sub>2</sub>O<sub>5</sub> is shown in Figure 1. It consists of layers of VO<sub>5</sub> square pyramids that share edges and corners, and sodium ions lying between the layers. There are two crystallographic vanadium sites, which form two kinds of  $VO<sub>5</sub>$  chain (A and B in Figure 1) along the *b*-axis. From the fact that  $\alpha'$ -NaV<sub>2</sub>O<sub>5</sub> is a mixedvalence  $(V^{4+}/V^{5+} = 1)$  oxide and the analysis of the V-O bond length and Na-V distance, it has been considered that the A and B chains are possibly  $V^{4+}O_5$  and  $V^{5+}O_5$ chains, respectively.<sup>5</sup> In this structure,  $\alpha'$ -NaV<sub>2</sub>O<sub>5</sub> is expected to be a quasi-1-D spin system because the magnetic  $V^{4+}O_5$  chains are isolated by the nonmagnetic  $V^{5+}\text{O}_5$  chains. Actually, the magnetic susceptibility for powder samples shows a typical temperature dependence for a 1-D magnetic system, as shown in Figure 2. The magnetic susceptibility can be excellently fitted with the Bonner-Fisher curve<sup>7</sup> with  $J/k_B = 560$ K and  $g = 2$ , where *J*,  $k_B$ , and  $g$  are the exchange constant, the Boltzmann constant, and the powder-averaged *g*-factor, respectively.6 Furthermore, the magnetic susceptibility rapidly decreases below 35 K with decreasing temperature, showing a slight upturn below 12 K. The magnetic susceptibilities along the *a*-, *b*-, and *c*-axes, measured with a single crystal, show sharp and isotropic reduction of magnetic susceptibility below 35 K, as shown in Figure 3. These results suggest that the transition is not a magnetic transition but a spin-Peierls transition.<sup>8</sup>

The spin-Peierls transition is one of the most interesting phenomena observed in low-dimensional quantumspin systems. It occurs in crystals containing linear (1-



**Figure 2.** Temperature dependence of magnetic susceptibility of  $\alpha'$ -NaV<sub>2</sub>O<sub>5</sub>. The solid line in the inset shows the susceptibility derived by subtracting the Curie contribution.



**Figure 3.** Temperature dependence of magnetic susceptibility along  $a$ -,  $b$ -, and  $c$ -axes in a single crystal of  $\alpha'$ -NaV<sub>2</sub>O<sub>5</sub>.

D) chains of spin-1/2 ions coupled by the antiferromagnetic exchange interaction. Below a spin-Peierls transition temperature  $T_{SP}$ , the structure of the underlying lattice changes so that the chains become dimerized. The dimerization in turn implies that the magnetic exchange interaction alternates in magnitude along the chain. The mechanism of the spin-Peierls instability is the coupling of the lattice phonons to the spins. Below *T*SP, the ground state is a nonmagnetic spin singlet, and a finite energy gap opens in the excitation spectrum. The spin-Peierls transition has been observed in organic  $compounds<sup>9-12</sup>$  and later in the inorganic metal oxide  $CuGeO<sub>3</sub>$ .<sup>2</sup>

A spin-singlet ground state in  $\alpha'$ -NaV<sub>2</sub>O<sub>5</sub> has been confirmed by nuclear magnetic resonance (NMR),<sup>13</sup> and the lattice dimerization and spin-gap formation below 35 K have been observed in X-ray and neutron scattering measurements.14,15 A single-crystal X-ray scattering experiment shows superlattice reflections with a lattice modulation vector  $q = (1/2, 1/2, 1/4).$ <sup>14</sup> The doubling of a unit cell along the *b*-axis implies lattice dimerization along the  $V^{4+}$  chains. The unit cell is also doubled along the *a*-axis, which intrinsically contains two  $V^{4+}$  chains. This situation is very similar to the case of  $CuGeO<sub>3</sub>$  in



**Figure 4.** Temperature dependence of (a) the superlattice intensity measured at  $\boldsymbol{Q} = (3/2, 1/2, 11/4)$  using X-ray scattering and (b) the gap energy  $\Delta$  measured at  $|Q| = 1.0$ Å<sup>-1</sup> using neutron scattering in  $\alpha'$ -NaV<sub>2</sub>O<sub>5</sub> (ref 14). The curves are guides for the eye.

**Table 1. Various Parameters of Spin-Peierls Systems**

systems	$J/k_B(K)$	$\Delta$ (K)	$T_{SP}$ (K)	$2\Delta/k_B T_{SP}$
$TTF-CuBDT9$	77	21	12	3.50
$TTF - AuBDT10$	68	3.7	2	3.70
$MEM$ -(TCNQ) $2^{11}$	106	28	18	3.11
SBTTF-TCNQC $l_2$ <sup>12</sup>	160	67	38	3.52
CuGeO <sub>3</sub> <sup>2</sup>	121	24.5	14	3.50
$\alpha'$ -NaV <sub>2</sub> O <sub>5</sub>	560	114	35.3	6.44

which a unit cell is also doubled along the *b*-axis containing two  $Cu^{2+}$  chains aligned perpendicular to the chain direction along the  $c$ -axis.<sup>16-18</sup> It is surprising that the unit cell quadruples in size along the *c*-axis, which is the stacking direction of the layers of the  $VO<sub>5</sub>$ pyramids connected two-dimensionally. The atomic displacement pattern, that is the crystal structure of the spin-Peierls phase, has not been solved. Figure 4 shows the temperature dependence of the superlattice intensity measured at  $\boldsymbol{Q} = (3/2, 1/2, 11/4)$  using X-ray scattering of the single crystal and the gap energy ∆ at  $|Q| = 1.0$  Å<sup>-1</sup> using neutron scattering of the powder sample.<sup>14</sup> Neither discontinuous change in intensity nor appreciable thermal hysteresis has been observed, which indicates that this transition is of the second order. The spin-Peierls transition in  $\alpha'$ -NaV<sub>2</sub>O<sub>5</sub> has also been confirmed by electron spin resonance (ESR).<sup>19</sup>  $\alpha'$ - $\text{NaV}_2\text{O}_5$  is the second inorganic spin-Peierls compound. The parameters of  $\alpha'$ -NaV<sub>2</sub>O<sub>5</sub> as the spin-Peierls system are shown in Table 1 together with those of another organic and inorganic spin-Peierls compounds. It is notable that the theoretically driven BCS-type formula in a weak coupling regime for the spin-Peierls transition,<sup>20</sup> 2∆/ $k_B T_{SP} = 3.53$ , holds well for the all-organic and inorganic spin-Peierls compounds except  $\alpha'$ -Na $\bar{V}_2O_5$ , for which the measure is 6.44. This exceptionally large value means that the transition observed in  $\alpha'$ -NaV<sub>2</sub>O<sub>5</sub> is not a conventional spin-Peierls transition but an exotic one. Anomalous behaviors that cannot be ex-



**Figure 5.** Temperature dependence of magnetic susceptibility of  $\alpha'$ -Na<sub>*x*</sub>V<sub>2</sub>O<sub>5</sub> (0.80  $\leq$  *x*  $\leq$  1.00).



**Figure 6.** Compositional dependence of Curie constant in  $\alpha'$ - $Na_{1-y}V_2O_5$ . The Curie constant was obtained from fitting the magnetic susceptibility to the Curie-Weiss law between 5 and 15 K. The dependence changes from the *y*/2 to *y*/12 around *y*  $= 0.03$  where the spin-Peierls transition disappears.

plained on the basis of simple 1-D spin-Peierls chains have been observed in the structure,  $^{14}$  NMR, $^{21}$  thermal conductivity, $22$  and dielectric constant $23$  measurements. In the connection with these anomalous behaviors, there are some arguments<sup>24</sup> that the crystal structure at room temperature is not a previously reported  $P2_1$ *mn* in the space group but a *Pmmn*. The latter space group is identical with that for  $V_2O_5$  and implies the presence of only one kind of V sites in contrast to two V sites in *P*2<sub>1</sub>*mn*. From these results, a possibility of charge ordering or charge disproportionation has been discussed for the transition in  $\alpha'$ -NaV<sub>2</sub>O<sub>5</sub>. A detailed mechanism of the transition has been an open question.

 $\alpha'$ -NaV<sub>2</sub>O<sub>5</sub> has a rather wide region of Na deficiency  $(0.8 \leq x \leq 1.0$  in  $\alpha'$ -Na<sub>*x*</sub>V<sub>2</sub>O<sub>5</sub>).<sup>25</sup> The spin-Peierls transition is suppressed by Na deficiency and vanishes around  $\alpha'$ -Na<sub>0.97</sub>V<sub>2</sub>O<sub>5</sub>.<sup>25</sup> Figure 5 shows the magnetic<br>susceptibility of the powdered  $\alpha'$ -Na<sub>-</sub>V<sub>2</sub>O<sub>c</sub> below 80 K susceptibility of the powdered  $\alpha'$ -Na<sub>x</sub>V<sub>2</sub>O<sub>5</sub> below 80 K. Sodium deficiency introduces nonmagnetic  $V^{5+}$  ions in



**Figure 7.** Logarithm of the electric resistivity versus  $1/T^{-1/2}$ of  $\alpha'$ -Na<sub>x</sub>V<sub>2</sub>O<sub>5</sub>. The inset shows the resistivity of  $\alpha'$ -Na<sub>x</sub>V<sub>2</sub>O<sub>5</sub> as a linear function of temperature. The resistivity is measured along *b*-axis parallel to the 1-D chains using single crystals.

the magnetic  $V^{4+}$  linear chains and cuts the chains. A Curie-like increase of magnetic susceptibility that is proportional to Na-deficiency has been observed in  $\alpha'$ - $Na<sub>x</sub>V<sub>2</sub>O<sub>5</sub>$  at low temperature, as shown in Figure 5. Evidence for a magnetic order, however, has not been observed in contrast to the Zn-doped  $CuGeO<sub>3</sub><sup>26-28</sup>$  or  $\rm SrCu_2O_3.^{29}$  This result indicates that  $\alpha'$ -NaV $_2$ O<sub>5</sub> is an<br>ideal 1-D magnetic system and the magnetic interchain ideal 1-D magnetic system and the magnetic interchain interaction is very weak. The Curie constants obtained from fitting the magnetic susceptibility to Curie-Weiss laws between 5 and 15 K are shown in Figure 6 as a function of *y* in  $\alpha'$ -Na<sub>1-*y*</sub>V<sub>2</sub>O<sub>5</sub>.<sup>25</sup> In this fitting, the Weiss<br>temperatures obtained were  $\sim$ 0 K to  $\sim$  –0.9 K in all temperatures obtained were ∼0 K to  $\sim$  -0.9 K in all samples. The dotted lines in Figure 6 represent the *y*/2 and  $y/12$  dependence, assuming free ions with  $S = 1/2$ associated with Na deficiency. At first, the Curie constant increases with a proportion of *y*/2 and then *y*/12 above  $y = 0.03$ . The turning point of  $y = 0.03$  corresponds to the composition where the spin-Peierls transition disappears. The introduction of a nonmagnetic ion into a magnetic linear chain affects the magnetic properties in a different manner in the spin-Peierls state and the 1-D magnetic uniform state, respectively. Such effects may be more remarkable in the state with a spingap than in the 1-D magnetic uniform state. Some theories predict that the compositional dependence of the Curie constant lies between *y*/4 and *y*/12 in the spinladder system with the spin gap.30,31

The stoichiometric  $\alpha'$ -NaV<sub>2</sub>O<sub>5</sub> is semiconductive. With Na deficiency,  $\alpha'$ -Na<sub>x</sub>V<sub>2</sub>O<sub>5</sub> becomes conductive but remains semiconductive. The electric resistivities of  $\alpha'$ - $Na<sub>x</sub>V<sub>2</sub>O<sub>5</sub>$  measured along the *b*-axis (the linear chain direction) using single crystals are shown in Figure 7.25 The temperature dependence of resistivity does not obey any activation type but shows a  $T^{-1/2}$  dependence, as shown in Figure 7. This dependence seems to be consistent with a variable range hopping in the 1-D system. This result suggests that the carriers are doped into the 1-D chain by Na deficiency but do not induce clean metallic behavior because an arbitrary small concentration of defects often leads to localization in a





 $CaV<sub>2</sub>O<sub>5</sub>$ 

**Figure 8.** Schematic crystal structure of orthorhombic  $CaV<sub>2</sub>O<sub>5</sub>$ .



**Figure 9.** Temperature dependence of magnetic susceptibility of  $CaV<sub>2</sub>O<sub>5</sub>$ . The solid line shows the susceptibility derived by subtracting the Curie contribution from impurities.

1-D material. This point is significant, differing from the doping effect in  $CuGeO<sub>3</sub>$  and  $SrCu<sub>2</sub>O<sub>3</sub>$ , where the doping or substitution of other cations for Cu has not resulted in the carrier doping but a long-range antiferromagnetic order.

#### **CaV2O5 (Spin-Ladder System with a Spin Gap)**

The structure of  $CaV<sub>2</sub>O<sub>5</sub>$  is orthorhombic, belongs to the space group *Pmmn*, <sup>32</sup> which is identical to that of  $V<sub>2</sub>O<sub>5</sub>$ , and consists of layers of  $VO<sub>5</sub>$  pyramids with Ca ions located between these layers, as shown in Figure 8.  $CaV<sub>2</sub>O<sub>5</sub>$  has a similar intralayer structure to that of



**Figure 10.** Temperature dependence of the *z*-component of the <sup>51</sup>V Knight shift  $(K<sub>z</sub>)$  in CaV<sub>2</sub>O<sub>5</sub> (ref 34). The solid line represents the values calculated using  $\Delta/k_B = 464$ K and  $K_{z,orb}$  $= 0.36\%$  in terms of the ladder model. The inset shows  $K - \chi$ plot with temperature ranging from 100 to 230 K.



**Figure 11.** Temperature dependence of spin-lattice relaxation rate  $(1/T_1)$  observed by <sup>51</sup>V NMR in CaV<sub>2</sub>O<sub>5</sub> (ref 34). The solid line represents the theoretically predicted values.

 $\alpha'$ -NaV<sub>2</sub>O<sub>5</sub>, but it is a monovalent oxide different from  $\alpha'$ -NaV<sub>2</sub>O<sub>5</sub>, and all vanadium ions are magnetic tetravalent  $V^{4+}$  ions in CaV<sub>2</sub>O<sub>5</sub>. The structure viewed along the *c*-axis is very similar to that of two-leg ladder cuprate  $SrCu<sub>2</sub>O<sub>3</sub><sup>3</sup>$  and therefore the basic structure of  $CaV<sub>2</sub>O<sub>5</sub>$  can be considered in two ways in terms of the exchange couplings. One is a ladder structure formed by the exchange coupling through the corners of the  $VO<sub>5</sub>$ pyramids. The other is a zigzag chain system, which is due to the exchange coupling across the edges of the VO<sub>5</sub> pyramids. Because the spins along the zigzag chain can be considered to be geometrically frustrated, a twoleg spin-ladder is a plausible spin system for  $CaV<sub>2</sub>O<sub>5</sub>$ . An energy gap originating from the inherent topological structure with  $S = 1/2$  for a two-leg ladder structure has been theoretically understood and then actually the formation of the spin singlet ground state without lattice distortion has been observed in the first two-leg ladder compound  $SrCu<sub>2</sub>O<sub>3</sub>$ .<sup>3,33</sup>

Figure 9 shows the raw data of magnetic susceptibility. The solid line in Figure 9 is the magnetic susceptibility derived by subtracting the contribution of impurities. The magnetic susceptibility has a maximum around 400 K, decreases with decreasing temperature, and reaches a small constant value below  $\sim$ 70 K. This behavior is a typical low-dimensional magnetic one. The spin-singlet ground state was directly confirmed by  $51V$ NMR.34 Figure 10 shows the temperature dependence of the *z*-component of the Knight shift (*Kz*). The parameter  $K_z$  increases with decreasing temperature, reflecting the decrease of the local spin susceptibility, and below 70 K it reaches a constant value of ∼0.3%, which is a typical value for a spin-singlet  $V^{4+}$  state. The *x* and *y* components of the Knight shift or  $K(K_X = 0.3\%$ ,  $K_y = 0.17\%$  do not change within the experimental error. The existence of an energy gap ∆ between nonmagnetic ground state and magnetic excited states was also confirmed from an activation type behavior of the spin-lattice relaxation rate  $(1/T_1)$ , as shown in Figure 11.

According to the ladder model, the *d*-spin susceptibility ( $\chi_{spin}$ ) and  $1/T_1$  are expressed as<sup>35</sup>

$$
\chi_{\rm spin} \propto T^{-1/2} \exp(-\Delta/k_{\rm B}T)
$$
  

$$
1/T_1 \propto \exp(-\Delta/k_{\rm B}T) [0.80908 - \ln(\omega_0/T)]
$$

where  $\omega_0$  is the nuclear resonance frequency. The fit of the experimental data for  $K_z$  and  $1/T_1$  to the relations just presented, using the relation  $K_{z,\text{spin}} \propto \chi_{\text{spin}}$ , where  $K_z = K_{z,\text{spin}} + K_{z,\text{orb}}$  is quite good, and the values of  $\Delta/k_B$ obtained from  $K_{z,\text{spin}}$  and  $1/T_1$  are 464 and 616 K, respectively. Because the exchange interaction can be estimated to be ∼600 K, the observed energy gap is much larger than the theoretical value of  $\Delta \approx J/2 \approx 300$ K in the ladder limit. There are some arguments that  $CaV<sub>2</sub>O<sub>5</sub>$  is significantly closer to the dimer limit with a large exchange interaction along the rung.<sup>36</sup>

In  $CaV<sub>2</sub>O<sub>5</sub>$ , V sites are substituted by nonmagnetic Ti<sup>4+</sup> ions to the extent of ~10%. Figure 12 shows the magnetic susceptibility of  $Ca(V_{1-x}Ti_x)_2O_5$ . The Curielike increase of magnetic susceptibility at low temperature is enhanced by the substitution of Ti, but any anomaly for a magnetic order has not been observed in the susceptibility curves, which is in contrast to the Zndoped  $SrCu<sub>2</sub>O<sub>3</sub>$ .<sup>29</sup>

### **MgV2O5 (Spin-Ladder System with a Spin Gap)**

 $MgV<sub>2</sub>O<sub>5</sub>$  is a tetravalent oxide like CaV<sub>2</sub>O<sub>5</sub>. Figure 13 shows the crystal structure of  $MgV_2O_5.^{37}$  The crystal structure consists of layers formed by edge- and cornershared  $V^{4+}O_5$  square pyramids with magnesium ions between the layers. The orthorhombic  $MgV<sub>2</sub>O<sub>5</sub>$  is very analogous to  $CaV<sub>2</sub>O<sub>5</sub>$  in structure, but the manner of layer stacking is somewhat different from that in  $CaV<sub>2</sub>O<sub>5</sub>$ ; that is, the layers in  $MgV<sub>2</sub>O<sub>5</sub>$  are alternatively stacked with a shift by *b*/2 along [010]. This result implies a doubling of the *c* parameter compared with  $CaV<sub>2</sub>O<sub>5</sub>$ . Because MgV<sub>2</sub>O<sub>5</sub> has an intralayer network of  $VO_5$  square pyramids similar to that in  $CaV_2O_5$ , it is



**Figure 12.** Temperature dependence of magnetic susceptibility of  $Ca(V_{1-x}Ti_x)_2O_5$  (0.00  $\leq x \leq 0.10$ ).



 $MgV<sub>2</sub>O<sub>5</sub>$ 

**Figure 13.** Schematic crystal structure of orthorhombic  $MgV<sub>2</sub>O<sub>5</sub>$ .

very interesting to determine whether  $MgV<sub>2</sub>O<sub>5</sub>$  is a spinladder system with a spin gap.

Figure 14 shows the temperature dependence of the magnetic susceptibility of  $MgV_2O_5.^{38}$  It has a characteristic of a low-dimensional magnetic system, that is, a broad maximum around 100 K. Below  $\sim$ 15 K, the magnetic susceptibility decreases more rapidly with decreasing temperature and shows a slight upturn below 5 K. This increase of magnetic susceptibility at low temperature may be due to magnetic impurities included accidentally. The magnetization curve up to



**Figure 14.** Temperature dependence of magnetic susceptibility of  $MgV<sub>2</sub>O<sub>5</sub>$ .



**Figure 15.** Magnetization curve of  $MgV_2O_5$  in a field up to 5 T measured using a SQUID magnetometer.

5 T at 2 K, shown in Figure 15, consists of two components. One component is a paramagnetic one and has a tendency to saturate at high external field. The other component linearly increases with increasing magnetic field in the magnetization. The former can be considered to originate from magnetic impurities. The concentration of the magnetic impurities can be estimated from the saturated magnetization to be ∼0.07% by assuming  $S = 1/2$ . The inflection of magnetic susceptibility around 15 K suggests a magnetic order, but the muon spin rotation (*µ*SR) experiments have revealed no evidence for a magnetic order down to the lowest temperature (2.5 K).<sup>39</sup> An excitation peak at  $\sim$ 2 meV has been observed in the inelastic neutron spectra measured with powder samples, as shown in Figure 16.40 The observed *Q*-dependence of the intensity at constant energy transfer shows peaks around the positions corresponding to the so-called  $(\pi,\pi)$  and  $(3\pi,\pi)$ , and the temperature dependence of the intensity can be well reproduced by a calculation assuming an excitation from singlet to triplet state.<sup>40</sup> These results strongly suggest a spin-singlet ground state in  $MgV<sub>2</sub>O<sub>5</sub>$ . Therefore, the linear component in the magnetization curve can be attributed to the orbital susceptibility (Van Vleck term), which can be estimated from the slope to be  $2.2 \times 10^{-4}$  $emu/V<sup>4+</sup>$ -mol. This value is rather large compared with those of spin-singlet states in other vanadium oxides.



**Figure 16.** Typical neutron energy scans in powdered  $MgV_2O_5$ (a) at  $|Q| = 1.27$  and 0.8 Å<sup>-1</sup> at 10 K and (b) at  $|Q| = 1.27$  Å<sup>-1</sup> at 10 and 33 K, and (c) temperature dependence of intensity of peak at 2 meV (ref 40).

Ohama et al.<sup>13</sup> pointed out that the magnetic susceptibility of the spin-Peierls state in  $\alpha'$ -NaV<sub>2</sub>O<sub>5</sub> is about twice as large as the temperature-independent term in the uniform state. Such large orbital susceptibilities may be a characteristic of the spin-singlet state of the  $V^{4+}$  ion with a pyramidal coordination of oxygen.

The spin-singlet ground state suggests that  $MgV_2O_5$ is either a spin-Peierls system similar to  $\alpha'$ -NaV<sub>2</sub>O<sub>5</sub> or



**Figure 17.** Magnetization curves of  $MgV_2O_5$  measured in steady magnetic fields up to 17 T at 1.5 and 4.2 K. The inset shows the d*M*/d*H* versus *H* curve at 1.5 K.

a two-leg spin-ladder system similar to  $CaV<sub>2</sub>O<sub>5</sub>$ . The possibility of spin-Peierls system may be ruled out from the structural characteristics, although the rapid decrease of magnetic susceptibility below 15 K is suggestive of a spin-Peierls transition. At present, there is no evidence of lattice distortion in the powder samples of MgV<sub>2</sub>O<sub>5</sub>. The small gap energy of ∼2 meV observed in the neutron scattering experiments suggests the possibility of the observation of a field-induced transition to a gapless state in high fields. Figure 17 shows the magnetization curves measured in steady magnetic fields up to 17 T at 1.5 and 4.2 K. $38$  The transition can be clearly seen at around  $H_c \sim 12.5$  T in the magnetization curves at 1.5 and 1.7 K. The magnetization increases almost linearly up to 8 T and above 12.5 T it increases more steeply. At 4.2 K, the slope in the magnetization changes more gently around the critical field. It is considered that the level crossing between the singlet ground state and the excited triplet state occurs at a critical field  $H_c$  corresponding to the excitation gap at zero field, and that the system is in a gapless magnetic state with a finite magnetic susceptibility above  $H_c$ . The excitation gap between the ground state and the lowest excited triplet state in a magnetic field *H* can be expressed as  $\Delta(H) = \Delta - gu_BH$ , where  $\Delta$  is the excitation gap at zero field and the  $\Delta/k_B$  of MgV<sub>2</sub>O<sub>5</sub> can be estimated from  $H_c$  to be ∼17 K, which is in agreement with  $\Delta/k_B \sim 20$  K from the neutron scattering studies. These results indicate that  $MgV_2O_5$  is a spinladder system with a spin-gap of  $\sim$ 17 K. This very small value should be contrasted with the much larger value ( $\sim$ 500 K) for CaV<sub>2</sub>O<sub>5</sub>.

## $\gamma$ **-LiV<sub>2</sub>O<sub>5</sub> (** $S = 1/2$  **Quasi-1-D System without Spin Gap)**

The orthorhombic  $\gamma$ -LiV<sub>2</sub>O<sub>5</sub> has a layer structure with lithium ions between the layers. In this structure there are two crystallographic vanadium sites that form two kinds of zigzag chains, the shaded and white zigzag chains in Figure 18. The valence states of vanadium ions were inferred from the results of structural analysis to be  $V^{4+}$  for the shaded zigzag chains and  $V^{5+}$  for the white zigzag chains.<sup>41</sup> Within the layers,  $V^{4+}O_5$  (shaded) zigzag chains are linked to  $V^{5+}O_5$  (white) zigzag chains by sharing corners, as shown in Figure 18. In the



**Figure 18.** Schematic crystal structure of orthorhombic  $\gamma$ -LiV<sub>2</sub>O<sub>5</sub>. The dark and white VO<sub>5</sub> square pyramids represent  $V^{4+}O_5$  and  $V^{5+}O_5$  pyramids, respectively.

structure of  $\gamma$ -LiV<sub>2</sub>O<sub>5</sub>, there are two kinds of V<sup>4+</sup>O<sub>5</sub> pyramids with apex oxygens above and below the sheet in Figure 18. Each kind of  $V^{4+}O_5$  pyramid forms an infinite linear chain by sharing a corner with the same kind of pyramid or one kind of pyramid forms an infinite zigzag chain by sharing an edge with the other kind of pyramid. Therefore, the magnetic structure can be regarded as a double-linear chain system or a zigzag chain system. In either case, *γ*-LiV<sub>2</sub>O<sub>5</sub> is expected to be a quasi-1-D-spin system because each double-linear chain or zigzag chain is isolated by the nonmagnetic  $V^{5+}O_5$  double-linear or zigzag chains.

Figure 19 shows the temperature dependence of the magnetic susceptibility of  $\gamma$ -LiV<sub>2</sub>O<sub>5</sub> measured in the powdered samples.42 The magnetic susceptibility has a broad maximum at  $\sim$ 200 K and shows a good fit to the equations for a  $S = 1/2$  1-D Heisenberg antiferromagnetic linear chain model<sup>7</sup> with  $J/k_B = 308$  K<sup>42</sup> and  $g = 1.8$ , as given by the solid line in Figure 19. These results are consistent with the characteristics of the crystal structure. The magnetic susceptibility extrapolated to the lowest temperature is much larger than that of Van Vleck paramagnetism of open shells of the  $V^{4+}$ ions, and any anomaly suggesting a magnetic order has not been observed in the susceptibility curve. It has been confirmed by 7Li NMR that the ground state of  $γ$ -LiV<sub>2</sub>O<sub>5</sub> is neither a spin-singlet state nor a magnetically ordered state down to 0.5 K.<sup>43</sup> γ-LiV<sub>2</sub>O<sub>5</sub> is a typical 1-D magnet in which the interchain exchange interac-



**Figure 19.** Temperature dependence of magnetic susceptibility of  $\gamma$ -LiV<sub>2</sub>O<sub>5</sub>. The solid line shows a fit to the equation for a  $S = 1/2$  1-D Heisenberg antiferromagnetic linear chain model with  $J/k_B = 308$  K,  $g = 1.8$ .



**Figure 20.** Temperature dependence of magnetic susceptibility of *γ*-Li<sub>*x*</sub>V<sub>2</sub>O<sub>5</sub> (0.90  $\leq$  *x*  $\leq$  1.00).

tion is very weak. Fujiwara et al.<sup>43</sup> have observed an anomalous behavior of spin-lattice relaxation rate that can be explained by considering the contribution from the staggered- and uniform-spin fluctuation.

*γ*-LiV<sub>2</sub>O<sub>5</sub> shows Li deficiency with somewhat narrower range compared with  $\alpha'$ -Na<sub>x</sub>V<sub>2</sub>O<sub>5</sub>. Figure 20 shows the magnetic susceptibility of the powdered *γ*-Li*x*V2O5 below 100 K. Li deficiency introduces nonmagnetic  $V^{5+}$  ions in the magnetic  $V^{4+}$  linear chains and cuts the chains. A Curie-like increase of magnetic susceptibility is observed at low temperature, but any evidence for a magnetic order has not been observed. The Curie constant obtained from fitting the magnetic susceptibility to a Curie law between 5 and 15 K, assuming free ion with  $S = 1/2$  associated with Li deficiency, increases with a proportion between *y*/5 and  $y/6$  in  $\gamma$ -Li<sub>1-*y*</sub>V<sub>2</sub>O<sub>5</sub>. The little dependence of Curie constant on the Li deficiency may also be caused from quantum effects, although *γ*-LiV<sub>2</sub>O<sub>5</sub> is not a system with a spin gap. This result is consistent with that observed from 51V NMR that the staggered moments are induced in a whole system by the existence of the open ends in the chains.<sup>44</sup>

*γ*-LiV<sub>2</sub>O<sub>5</sub> is more conductive than  $\alpha'$ -Na<sub>*x*</sub>V<sub>2</sub>O<sub>5</sub> but is semiconductive. The electric resistivity of  $\gamma$ -Li<sub>x</sub>V<sub>2</sub>O<sub>5</sub> measured along the *b*-axis (the linear chain direction)



**Figure 21.** Logarithm of the electric resistivity versus  $1/T^{-1}$ of  $\gamma$ -Li<sub>x</sub>V<sub>2</sub>O<sub>5</sub>. The inset shows the resistivity of  $\gamma$ -Li<sub>x</sub>V<sub>2</sub>O<sub>5</sub> as a linear function of temperature. The resistivity is measured along *b*-axis parallel to the 1-D chains using single crystals.



 $CsV<sub>2</sub>O<sub>5</sub>$ 

**Figure 22.** Schematic crystal structure of monoclinic  $CsV<sub>2</sub>O<sub>5</sub>$ . The  $VO<sub>5</sub>$  (shaded) square pyramids and the  $VO<sub>4</sub>$  (white) tetrahedra are occupied by  $\hat{V}^{4+}$  and  $V^{5+}$  ions, respectively.

using single crystals is shown in Figure 21. The resistivity of stoichiometric  $γ$ -LiV<sub>2</sub>O<sub>5</sub> shows an activation type behavior, and the energy gap was estimated to be ∼0.32 eV. The resistivity of  $\gamma$ -Li<sub>x</sub>V<sub>2</sub>O<sub>5</sub> decreases with Li deficiency at 300 K but  $\gamma$ -Li<sub>x</sub>V<sub>2</sub>O<sub>5</sub> remains semiconductive. The temperature dependence of the resistivity of  $\gamma$ -Li<sub>x</sub>V<sub>2</sub>O<sub>5</sub> does not obey any activation



**Figure 23.** Temperature dependence of magnetic susceptibility of  $CsV<sub>2</sub>O<sub>5</sub>$  derived by subtracting the Curie contribution from impurities. The solid line shows a fit to the equation for  $S = 1/2$  Heisenberg dimer model with  $J/k_B = 146$  K and  $g =$ 1.8. The inset shows the raw data of magnetic susceptibility.

types, as shown in Figure 21. This result suggests that the carriers are possibly doped into the 1-D linear chains, but the conducting behavior of the doped samples is not of a variable range hopping and is more complex.

## **CsV2O5 (Dimer System)**

The crystal structure of  $CsV<sub>2</sub>O<sub>5</sub>$  is somewhat different from those of  $\gamma$ -LiV<sub>2</sub>O<sub>5</sub> and  $\alpha'$ -NaV<sub>2</sub>O<sub>5</sub>. The structure of monoclinic  $CsV<sub>2</sub>O<sub>5</sub>$  is also a layer one with cesium ions between the layers, as shown in Figure 22.42,45 The vanadium atoms, on two distinct crystallographic sites, exhibit two types of coordination polyhedra. One type is in a square pyramid formed by five oxygens, whereas the other is tetrahedrally surrounded by four oxygens. The bond valence analysis reveals that the V sites in the  $VO<sub>5</sub>$  (shaded) square pyramids and the  $VO<sub>4</sub>$  (white) tetrahedra are occupied by  $V^{4+}$  and  $V^{5+}$  ions, respectively.45 Two square pyramids share an edge in such a way that each terminal oxygen is in above and below the plane formed by the equatorial. These isolated double square pyramids are linked by the  $VO<sub>4</sub>$  tetrahedra to form the layer.

The temperature dependence of the magnetic susceptibility of  $CsV<sub>2</sub>O<sub>5</sub>$  is shown in Figure 23.<sup>42</sup> The magnetic susceptibility has a maximum at ∼90 K. The upturn of magnetic susceptibility below 20 K is considered to be due to the existence of impurities and/or free ions caused by defects. In CsV<sub>2</sub>O<sub>5</sub>, the magnetic V<sup>4+</sup>O<sub>5</sub> square pyramids form a dimer instead of a linear chain in  $\gamma$ -LiV<sub>2</sub>O<sub>5</sub> or  $\alpha'$ -NaV<sub>2</sub>O<sub>5</sub> and the dimers are isolated by the nonmagnetic  $V^{5+}O_4$  tetrahedra, as already mentioned. The magnetic susceptibility for the  $S = 1/2$ Heisenberg dimers is given as, 46

$$
\chi_{\text{raw}} = \chi_{\text{CVO}} + \chi_{\text{imp}} =
$$
  

$$
\frac{N g^2 \mu_{\text{B}}^2}{k_{\text{B}} T} \frac{1}{3 + \exp\left(-\frac{2|J|}{k_{\text{B}} T}\right)} + \chi_{\text{o}} + \chi_{\text{imp}}
$$

where  $\chi_{\text{CVO}}$  and  $\chi_{\text{imp}}$  are the contribution of magnetic susceptibility from pure  $CsV<sub>2</sub>O<sub>5</sub>$  and impurities, respectively, and *g* and *J* are the powder-averaged *g*-factor

**Table 2. Vanadate Family as Spin-gap Systems**

vanadate	quantum spin system	sharing of $V^{4+}\overline{O}_5$	J(K)	$\Delta$ (K)
$\alpha'$ -NaV <sub>2</sub> O <sub>5</sub>	spin-Peierls	corner	560	114
CsV <sub>2</sub> O <sub>5</sub>	dimer	edge	146	160
$\gamma$ -LiV <sub>2</sub> O <sub>5</sub>	1-D zigzag chain	corner/edge	310	
CaV <sub>2</sub> O <sub>5</sub>	ladder	corner/edge		600
MgV <sub>2</sub> O <sub>5</sub>	ladder	corner/edge		17

and the exchange constant, respectively. The raw data  $(\chi_{\text{raw}})$  of magnetic susceptibility observed in  $\text{CsV}_2\text{O}_5$  can be excellently fitted to this equation with  $J/k_B = 146$  $K^{42}$  and  $g = 1.8$ , as shown in the solid line in Figure 23. The subtraction of  $\chi_{\text{imp}}$  from  $\chi_{\text{raw}}$  gives a small constant value of  $\chi_0 = 8 \times 10^{-5}$  (emu/mol) below 30 K. This value is comparable to the magnetic susceptibility of the insulating phase of  $\rm VO_{2}^{47}$  and the ground state in the spin-Peierls compound  $\alpha'$ -NaV<sub>2</sub>O<sub>5</sub> in which spin-singlet  $V^{4+}-V^{4+}$  pairs are formed. This result indicates that the ground state of  $CsV<sub>2</sub>O<sub>5</sub>$  is a spin-singlet state. The spin-gap energy can be estimated from the NMR experiments to be the same order ( $\Delta$  = 160 K) of the exchange interaction.

#### **Overview**

All of vanadium oxides reviewed here are lowdimensional, spin-1/2 magnets that belong to various kinds of quantum-spin systems and are spin-gap systems except  $\gamma$ -LiV<sub>2</sub>O<sub>5</sub>. They are summarized in Table 2. The characteristic low-dimensional spin structures of these compounds are formed by sharing edges and/ or corners of  $V^{4+}O_5$  square pyramids in the manner that each apical oxygen is located in the opposite side from the basal plane in the edge-sharing pyramids and is in the same side in the corner-sharing pyramids.  $\alpha'$ - $NaV<sub>2</sub>O<sub>5</sub>$  includes 1-D chains formed by only cornersharing  $V^{4+}O_5$  square pyramids, whereas  $CsV_2O_5$  includes dimers formed by only edge-sharing  $V^{4+}O_5$  square pyramids. The observed exchange integral  $J$  of  $\alpha'$ - $NaV<sub>2</sub>O<sub>5</sub>$  is much larger than that of  $CsV<sub>2</sub>O<sub>5</sub>$ . This means that the exchange interaction is much stronger in the corner-sharing  $\bar{V}^{4+}O_5$  square pyramids than in the edge-sharing pyramids. *γ*-LiV<sub>2</sub>O<sub>5</sub> has 1-D zigzag chains in which the spins interact through both the edges and the corners of  $V^{4+}O_5$  square pyramids. It should be noticed that the exchange integral of 310 K observed in  $\gamma$ -LiV<sub>2</sub>O<sub>5</sub> is very close to the difference of *J* between  $\alpha'$ -NaV<sub>2</sub>O<sub>5</sub> and CsV<sub>2</sub>O<sub>5</sub>. The exchange integrals of  $CaV<sub>2</sub>O<sub>5</sub>$  and  $MgV<sub>2</sub>O<sub>5</sub>$  cannot be estimated from the temperature dependence of magnetic susceptibility because of the spin-ladder structure.  $CaV<sub>2</sub>O<sub>5</sub>$  and  $MgV<sub>2</sub>O<sub>5</sub>$  are spin-ladder systems with spin gaps and the observed energy gap is much larger in  $CaV<sub>2</sub>O<sub>5</sub>$  than in  $MgV<sub>2</sub>O<sub>5</sub>$ . This difference may be related to the difference of the local structure; that is, the difference of the exchange interaction.



**Figure 24.** The definition of the distortion  $(D)$  of  $V^{4+}O_5$  square pyramid and the distance  $(d_H)$  of the V<sup>4+</sup> ion from the basal plane.



**Figure 25.** Crystal field levels of a  $V^{4+}$  ion in a regular  $VO_5$ pyramid with the equi-distance of  $d_{V-O} = 1.9$  Å, calculated from a simple point charge model, as a function of the distance of the  $V^{4+}$  ion from the basal plane (ref 48).

The various local, structural parameters derived from the crystal structure at room temperature are summarized in Table 3. In all compounds, the  $V^{4+}O_5$  square pyramids are distorted and the basal plane is not flat. The parameter *D* in Table 3, which shows a degree of distortion of the basal plane, is expressed as the ratio of the distance  $(d_1)$  of  $V^{4+}$  ions from the center of diagonal line along the *a*-axis to that  $(d_2)$  along the  $b$ -axis, as shown in Figure 24. The parameter  $d_H$ (distance of the  $V^{4+}$  ions from the basal plane) in Table 3 is the average of  $d_1$  and  $d_2$ . The basal plane of the V<sup>4+</sup>O<sub>5</sub> square pyramid is distorted in *γ*-LiV<sub>2</sub>O<sub>5</sub> and CsV<sub>2</sub>O<sub>5</sub>, whereas it is rather flat in  $\alpha'$ -NaV<sub>2</sub>O<sub>5</sub>, CaV<sub>2</sub>O<sub>5</sub>, and  $MgV_2O_5$ . Ohama et al.<sup>48</sup> calculated the crystal field splitting of a  $V^{4+}$  ion in a regular  $VO_5$  pyramid with the equidistance of  $d_{V-O} = 1.9$  Å from a simple point charge model. The crystal field levels obtained are shown in Figure 25 as a function of the distance of the  $V^{4+}$  ions from the basal plane. The ground state of  $d$ levels changes from the doublet *dyz*, *dzx* to the singlet  $d_{xy}$  upon increasing the shift of the  $V^{4+}$  ion from the basal plane. The results indicate that the ground state is  $d_{xy}$  in this vanadate family, because the averaged distance of  $V^{4+}$  ion from the basal plane is scattered around  $0.6-0.7$  Å in all compounds, although the real

**Table 3. Structural Parameters***<sup>a</sup>*

		<b>Ichain</b>			∟chain		edge		
vanadate	$d_{V-O}$	$\theta_{Q-V-Q}$	$d_{V-V}$	$d_{V-O}$	$\theta_{\text{O}-\text{V}-\text{O}}$	$d_{V-V}$	$d_{V-V}$	$d_H$	D
$\alpha'$ -NaV <sub>2</sub> O <sub>5</sub>	1.962	23.06	3.611					0.7231	1.134
CsV <sub>2</sub> O <sub>5</sub>							3.073	0.5771	1.684
$v$ -LiV <sub>2</sub> O <sub>5</sub>	1.960	23.06	3.004				3.004	0.6533	1.424
CaV <sub>2</sub> O <sub>5</sub>	1.949	22.36	3.605	1.905	23.55	3.492	3.025	0.6564	1.298
MgV <sub>2</sub> O <sub>5</sub>	1.957	19.43	3.692	1.971	31.22	3.372	2.983	0.6712	0.942

*a* Distances (*d*) are in Å and Angles ( $\theta$ ) are in degrees.



**Figure 26.** Schematic representation of the frustrated coupledladder system.

**Table 4. Estimated Exchange Integrals in Kelvin***<sup>a</sup>*

vanadate	$J_1$	$J_2$	J <sub>2</sub>	$J_2/J_1$	J <sub>2</sub> /J <sub>1</sub>
$\alpha'$ -NaV <sub>2</sub> O <sub>5</sub>		530			
CsV <sub>2</sub> O <sub>5</sub> $\gamma$ -LiV <sub>2</sub> O <sub>5</sub> <sup>b</sup>	146 $183^b$	$568^b$		3.1 <sup>b</sup>	
CaV <sub>2</sub> O <sub>5</sub> MgV <sub>2</sub> O <sub>5</sub>	170 201	587 565	730 511	3.5 2.8	4.3 2.5

*<sup>a</sup>* Reference 50. *<sup>b</sup>* Present work.

VO5 pyramid is not a regular VO5 pyramid with equi $d_{V-O}$  and is distorted. Actually, the observed anisotropy of the NMR and the electric field gradient (EFG) indicates that the  $d_{XY}$  like orbital is occupied in  $\alpha'$ - $\rm Na V_2O_5$  and  $\rm Ca V_2O_5.^{48}$ 

Marini and Khomskii<sup>36</sup> discussed a large spin gap in  $CaV<sub>2</sub>O<sub>5</sub>$  from the formation of tightly bound dimers caused by V ions shift and corresponding orbital ordering. In their model, a *d*-electron occupies the *zx*-like orbital and V ions form dimers along the rungs. The out-of-plane position of V ions leads to an extra contribution to the exchange that is due not only to  $\pi$ - but also to *σ*-overlap. The strong exchange interaction of the order of the spin gap is due to *σ*-overlap. This model seems to explain a large spin gap or strong exchange interaction but the occupied *d*-orbital (*zx*-like orbital), which is essential in their model, is inconsistent with the NMR results.

Normand et al*.* <sup>49</sup> studied the theoretical magnetic phase diagram of the frustrated coupled-ladder structure and Millet et al*.* <sup>50</sup> discussed the vanadate family according to the analysis of the model performed by Normand et al.49 Figure 26 shows the schematic representation of the frustrated coupled-ladder system. Millet et al.50 estimated the exchange integrals of  $CaV<sub>2</sub>O<sub>5</sub>$  and  $MgV<sub>2</sub>O<sub>5</sub>$  based on the structural and magnetic information, assuming that these depend only on the local geometry of the bonds. The results are shown in Table 4 together with our estimation for  $\gamma$ -LiV<sub>2</sub>O<sub>5</sub>, where the exchange integrals of CsV<sub>2</sub>O<sub>5</sub> and  $\alpha'$ -NaV<sub>2</sub>O<sub>5</sub> are used as a measure to estimate  $J_1$  and  $J_2$ (or  $J_2$ ) in other members, respectively. According to their explanation, the ratio  $J_2/J_1 = 4.3$  clearly puts  $CaV<sub>2</sub>O<sub>5</sub>$  in the ladder limit with a large gap, whereas  $J_2/J_1 = 2.5$  with  $J_2/J_1 = 2.8$  puts MgV<sub>2</sub>O<sub>5</sub> very close to the helical ordered-hence gapless-phase and the system is thus expected to have a very small gap.

These vanadate family members belong to various kinds of quantum-spin systems and have provided a stage where various quantum spin phenomena can be investigated systematically, similar to the cuprates. For further investigation it is necessary to grow single crystals that have enough size to measure anisotropic properties. Large crystals of  $\alpha'$ -NaV<sub>2</sub>O<sub>5</sub> and  $\gamma$ -LiV<sub>2</sub>O<sub>5</sub> have been successfully grown<sup>8</sup> but others have not been yet. The information derived from the systematic study will serve as fundamental data for materials design or for developing new materials. At present, the author has no idea of applications of these quantum-spin systems, but suggests that quantum spin phenomena might receive attention in connection with potential devices called "spinics" (which is a parody on "electronics") in the next generation.

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